

Green's Functions for Ordinary Differential Equations

Dr. Laure Gouba

Abdus Salam International Centre for Theoretical Physics, Trieste, Italy
Email: laure.gouba@gmail.com

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Introduction

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This mini course is for everyone who is interested in the topic. It is assumed that the audience is familiar with elementary differential and integral calculus.